Rutgers University Math 152

Section 10.10: Applications of Taylor Series - Worksheet

1. Use Maclaurin series to compute the following limits.

(a)
$$\lim_{x \to 0} \frac{e^{-2x^2} - \cos(2x)}{x^2 \ln(1+5x) - 5x^3}.$$
(b)
$$\lim_{x \to \infty} x^3 \left(\tan^{-1}\left(\frac{4}{x}\right) - 2\sin\left(\frac{2}{x}\right) \right).$$
(c)
$$\lim_{x \to 0} \frac{\sin(x^6)}{\cos(x^3) - 1}.$$
(d)
$$\lim_{x \to \infty} x^2 \left(5\ln\left(1+\frac{3}{x}\right) - 3\ln\left(1+\frac{5}{x}\right) \right).$$

2. Use Maclaurin series to write each integral below as the sum of an infinite series of numbers (your series should not contain x).

(a)
$$\int_0^{1/2} \cos(5x^2) dx$$
. (b) $\int_0^1 x^3 e^{-4x^3} dx$. (c) $\int_0^{1/3} x^7 \sin(2x^5) dx$.

- 3. (a) Use Maclaurin series to write the integral $I = \int_0^1 e^{-x^2} dx$ as the sum of an infinite series of numbers.
 - (b) Use the Alternating Series Estimation Theorem to find how many terms of the series found in (a) need to be summed in order to obtain an approximation of I with an error of less than 10^{-5} .