Error Mitigating Quantum Computations of Molecular Ground States

Abstract

Quantum Computers have the potential to solve chemistry problems of great industrial importance but near term devices are susceptible to errors. Thus, error mitigation techniques like Richardson Extrapolation are being explored to reduce the effect of errors. In this project, we compare the Richardson method with a simpler polynomial-fitting method to determine the zero noise ground state energy of the hydrogen molecule. Results and implications are discussed.



- superposition and entanglement to perform computations. • Recently, a hybrid quantum-classical algorithm – Variational Quantum Eigensolver (VQE) – has been devised which optimizes electrons in molecular orbitals to minimize the energy of molecular systems.
- However quantum computers are highly susceptible to errors due to imperfect qubits and gates.
- Constrained by the number of qubits to correct those errors, error mitigation techniques are being explored as an alternative to reduce the effects of errors.

Dissassociation Curves for Hydrogen Molecule



Fig 2: As we stretch 2 hydrogen atoms apart, we compute the minimum energy of the molecule using VQE on IBM's noisy quantum computer at London and compare it with the exact energy. Minimum occurs at 0.74 Angstroms.

Error Mitigation Techniques

Richardson Extrapolation: Noisy expectation value of any observable can be expressed as

 $E(\lambda) = E^* + a_1\lambda + a_2\lambda^2 + a_3\lambda^3 + \dots$

- where λ is the noise rate and E^* is the noise free expectation value. By cancelling out terms from the expansion, we can better our approximation. For such cancellations, we need to obtain noise amplified energies as shown in Fig 4a.
- **Polynomial Extrapolation:** Given energies at various noise scaling factors, we can fit polynomial function using nonlinear least squares and then evaluate those functions at zero noise.



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Results

Fig 3: Using noise model simulation of IBM's quantum computer at London, we compare Richardson technique with polynomial fitting technique in improving the VQE-computed ground state energy of the Hydrogen molecule. Noise was amplified while optimizing in the VQE process.



Fig 3a : As the noise is increased the deviation of

the calculate ground state energy from the exact

• Polynomial Extrapolated Energy

• Richardson Extrapolated Energy

value increases.

1.0 -

0.5

-0.5

-1.0





Fig 3c : Uncertainty of zero noise energy extrapolated by Richardson is worse than that by lower degree polynomials.

Degree of Polynomial

Fig 4: Using IBM's quantum computer at London, we compare Richardson technique with polynomial fitting technique in improving the VQE-computed ground state energy of the Hydrogen molecule. Noise was amplified after optimizing parameters in VQE.











Fig 3b : Using Least Squares to fit polynomial functions through the noise energies.

Fig 3d : Zooming into Fig 3c, zero energy extrapolated by Richardson is worse than that of lower degree polynomials.

Fig 4b: Zero Noise energy extrapolated by Richardson is both worse in precision and accuracy than that extrapolated by lower degree polynomial fits.



Conclusion & Future Work

- shown by Fig 3c, 3d and 4b.
- order to obtain an improved fit. accuracy.



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Methods

To compare the Richardson and the polynomial fitting techniques, we ran VQE algorithm on the hydrogen molecule and extrapolated the results. • Noise could be amplified during the optimization phase of VQE or afterwards.

• Since the dominant source of noise on IBM's quantum computers are two qubit gates, we can add redundant CNOT gates to amplify the noise rate.

Fig 5: The addition of a pair of noisy CNOT gates triples the noise rate λ .

Zero noise extrapolated energy obtained via polynomial fitting is more precise and accurate than that obtained via Richardson technique, as

We plan to improve the technique by amplifying the noise in finer steps in

Also, zero noise extrapolated energies we obtained are not within chemical

We will then investigate other error mitigation strategies such as probabilistic error cancellation and quantum subspace expansion to obtain improved accuracy of the ground state energy



Fig 6: We also plan to apply techniques to more these complex molecules like Lithium Hydride and Water.

Acknowledgements

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