Financial Frictions and Unconventional Monetary Policy in Emerging Economies

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Chang and Velasco (Rutgers and Columbia) Unconventional Monetary Policy

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- New liquidity and credit facilities, manipulation of reserve requirements, intervention in foreign exchange market.
- This was the case in developed and emerging economies, including inflation targeters (see e.g. Chang 2007, Céspedes, Chang and Velasco 2014)

⇒What are the implications of unconventional policies in open economies?
⇒How do they compare and interact with conventional policies?
⇒Are unconventional policies effective all the time or only during crises?
⇒How can we reconcile unconventional policy with inflation targeting?
⇒Is the analysis the same in advanced economies *vis a vis* emerging ones?

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- Uses it to analyze the mechanics of conventional and unconventional policy and to derive answers to the preceding questions

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- Financial Intermediaries borrow abroad subject to a debt constraint
- Domestic Frictions as well: Equity Constraint
- The two constraints combine to give an economy-wide external debt limit

- Endogenous Spread
- Amplification of Shocks
- Financial Shocks, which can be both domestic or external, can lead to Sudden Stops
- The external balance condition emerges as the main driver of the adjustment process

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- With *flexible* exchange rates and a policy of stabilizing the interest rate, consumption is constant, adverse shocks are met with a steep devaluation, and output and exports increase
- *Currency mismatches* affecting the equity constraint add amplification, persistence, and volatility under flexible rates (but make no difference under fixed rates)

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- Unconventional policies affect equilibria if and only if financial constraints bind
- Because of leverage, liquidity facilities are more powerful than direct lending
- Unconventional policies can be used to offset shocks completely, but are feasible only if FX reserves are sufficient
- In contrast, conventional policy always involves some trade-off between demand adjustment and real depreciation



- Equity injections are a special case of liquidity facilities
- Sterilized FX intervention is equivalent to either direct lending or liquidity facilities

The Model

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- Consumption an aggregate of those two goods
- Home good an aggregate of varieties produced with only labor (typical monopolistic competition setting)
- Foreign demand for the domestic good is xe^χ_t, where e_t is the real exchange rate

Hence market clearing for the home good is

$$y_t = \alpha e_t^{1-\alpha} c_t + x e_t^{\chi}$$

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Image: A matrix



Financial Flows

• Banks lend to domestic households at loan rate ϱ_t

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- Bank loans = Funding from foreign lenders plus "equity":

$$l_t = d_t + k_t$$

Banks' Credit Limit

Simple constraint on the bank's debt:

 $d_t \leq \theta k_t$

Equivalently,

 $l_t \leq (1+\theta)k_t$
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Simple constraint on the bank's debt:

$$d_t \leq \theta k_t$$

Equivalently,

$$l_t \leq (1+\theta)k_t$$

• The two constraints must bind if $\varrho_t > \rho$ (i.e. if there is a positive spread)

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- The equity constraint reflects unmodeled domestic frictions
- It will bind if and only if $\varrho_t > \rho$
- So, the equity constraint binds iff the bank's external constraint binds as well

The household maximizes lifetime utility subject to

$$e_t^{-\alpha}b_t + k_t - l_t$$

$$= (1 + r_{t-1})e_t^{-\alpha}b_{t-1} + (1 + \omega_{t-1})(1 + \rho)k_{t-1}$$

$$- (1 + \varrho_{t-1})l_{t-1} + e_t^{-\alpha}(w_t n_t + v_t) + z - e_t^{-\alpha}c_t$$

and the equity constraint

$$k_t \leq \widetilde{k}$$

The household's solution is given by a labor supply condition

$$(1 - \epsilon^{-1})e_t^{-(1-\alpha)}c_t^{-1} = \eta y_t, \tag{1}$$

the consumption Euler equation

$$c_{t+1} = c_t \beta(1+r_t), \qquad (2)$$

and the arbitrage equation (between bonds and bank loans)

$$1 + r_t = (1 + \varrho_t) \left(\frac{e_{t+1}}{e_t}\right)^{\alpha}, \qquad (3)$$

The household's budget constraint becomes the external balance condition

$$(1-\alpha)e_t^{-\alpha}c_t - [z + xe_t^{\chi-1}] = d_t - (1+\rho)d_{t-1}$$

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And the foreign debt must satisfy:

$$0 \leq d_t \leq \theta \widetilde{k} \text{ if } \varrho_t = \rho$$
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• The foreign debt limit combines domestic and external frictions

Focus on *constrained* steady states, in which $\bar{\varrho} > \rho$, so that

$$ar{k} = ar{k} \ ar{d} = heta ar{k}$$

 \implies The ss amount of debt is determined *solely* by heta and $ilde{k}$

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A necessary condition for a constrained ss is eta(1+
ho) < 1 since

$$1+\overline{r}=1+\overline{\varrho}=\beta^{-1}.$$

Real variables are given by

$$ar{c} = -ar{e}^{lpha}
ho \overline{d} + ar{e}^{-(1-lpha)} \overline{y} + ar{e}^{lpha} z$$
 $(1 - \epsilon^{-1}) \overline{e}^{-(1-lpha)} \overline{c} = \eta \overline{y},$
 $\overline{y} = lpha \overline{e}^{(1-lpha)} \overline{c} + x \overline{e}^{\chi}.$

Special case: $\rho = 0$. Then the above eqs. do not depend on $\overline{d}!$

Dynamics Under Flexible Prices

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- **②** A fall in the bank's external constraint coefficient $\theta' < \theta$
- **③** A reduction in the equity bound to $\tilde{k}' < \tilde{k}$

The external balance constraint becomes

$$(1-\alpha) e^{-\alpha} c - (x e^{\chi - 1} + z) = s$$

with

$$s \equiv \tilde{k}'(\theta' - \theta) + \theta(\tilde{k}' - \tilde{k}) + (z' - z) < 0$$

Image: A mathematical states and a mathem

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• A sudden stop

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- So the only possibility is to generate a trade surplus
- Financial shocks result in the need for immediate deleveraging and also require an immediate trade surplus

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is a locus of combinations (c, e) that is shifted by the shock s.

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- Hence a negative s requires some combination of a fall in c or increase in e
- Assuming flexible prices, this is given by market clearing and optimal labor supply condition



External Balance

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External Balance: An Adverse Shock



Adjustment With Flexible Prices

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• Consumption falls

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- Real depreciation

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- Output increases
In response to one of the shocks under analysis:

- Consumption falls
- Real depreciation
- Output increases
- The loan rate ϱ goes up (to choke increased demand for loans)

Adjustment to *favorable* shocks can be more gradual, since financial constraints can *cease* to bind.

(Conventional) Monetary Policy

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- Focus on the traditional "fix versus flex exchange rate" question

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- In short, fixed exchange rates are contractionary



Adjustment Under Nominal Rigidities : Exchange Rate Peg



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Adjustment Under Nominal Rigidities: Interest Peg

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- So flexible exchange rates (with a fixed real interest rate) are expansionary

The Role of Currency Mismatches

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Suppose that the equity constraint is

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- Flexible exchange rates are less expansionary (as depreciation reduces the amount of foreign credit)
- Amplification and volatility
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- Currency mismatches make flexible rates relatively less appealing

Unconventional Policies

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$$(1 - \alpha) e_t^{1 - \alpha} c_t - e_t (d_t + l_t^g) = -e_t (1 + \rho) (d_{t-1} + l_{t-1}^g) + x e_t^{\chi} + e_t (z + \rho f)$$

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• And this is the only impact on the equilibrium conditions

Implications

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- In steady state,

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 $\ \, {\rm O} \ \, {\rm If} \ \, \rho = {\rm O}, \ {\rm the \ external \ \, constraint \ is} \ \,$

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with $\hat{z}_t = z + l_t^g - l_{t-1}^g$. So direct lending effectively "controls" z

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③ If ho = 0, the external constraint is

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- It is the *change* in I_t^g which matters
- Limit to this: international reserves. $(I_t^g I_{t-1}^g \le f I_{t-1}^g = \text{amount} \text{ of FX reserves})$

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This implies that

$$I_t \leq (1+\theta)k_t + (1+\phi)d_t^g$$

The external constraint becomes

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 \Rightarrow This is just as with direct lending

 \Rightarrow But discount lending also implies

$$d_t \leq \theta k_t + \phi d_t^g$$

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Intuition: leverage

If the central bank takes equity in the financial intermediary, the effect is the same as with liquidity facilities, except that $\phi = \theta$

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 \Rightarrow Conventional policy always involves trade-offs

On Sterilized FX Intervention

• Sterilized FX intervention always results in a change in international reserves offset by central bank credit

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- Hence it is equivalent to one of the operations discussed already (Céspedes, Chang, and Velasco 2015)

9 Sterilized FX Intervention has real effects iff financial constraints bind

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- On Their effects depend only on the nature of the sterilizing operation

- **1** Sterilized FX Intervention has real effects iff financial constraints bind
- Inter a start of the sterilizing operation
- These arguments are independent of portfolio balance considerations or signaling effects

Final Remarks

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• Endogenizing the equity constraint

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- Allowing for the coexistence of direct finance as well as intermediated finance (Chang, Fernández, Gulan 2015)

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- Allowing for the coexistence of direct finance as well as intermediated finance (Chang, Fernández, Gulan 2015)
- Optimal reserves accumulation and utilization