21. Shipping crates A square-based, box-shaped shipping crate is designed to have a volume of 16 ft³. The material used to make the base costs twice as much (per square foot) as the material in the sides, and the material used to make the top costs half as much (per square foot) as the material in the sides. What are the dimensions of the crate that minimize the cost of materials?

06T. F. -> 2var. ha. Costrant eq. J Abs. ~- 1-0x Local - ass.

Sq. based box diff. materials

V-> 16 ft? for base, sides, top MIN. Get of the materials

4 5 des

 $V = x \cdot x \cdot y = x \cdot y = 16 \text{ ft}^3$

Constraint C -> Ost (per sq. ft.) of the material to make the stoles

base mot costs 2 x nat for the solu Top mat. Osts 1/2 x mot for the sides

Area of a base -> x2 4 × Area of the sides > Area of the top of X2

F. Total Cost = 2c.x2 + 4.c.xy + c.x2

Cost forthe cost for ost for the top

base all sides

Obj. Total Cost = 2c·x² + 4·c·xy + c.x² MIN Extraint cost forthe cost for ost forthe cost forthe cost

> Re-write the ost (ost.) f. $C(x,y) = 2cx^{2} + cx^{2} + 4cxy$ c(x)

$$C(x) = 2c \cdot x^{2} + \frac{c}{2} \cdot x^{2} + 4c \cdot x \cdot \frac{16}{x^{2}}$$

$$= \frac{5}{2} c x^{2} + \frac{64c}{x} = c\left(\frac{5x^{2}}{2} + \frac{64}{x}\right)$$

Shipping Crates 3

Therefore 24, 2020 9-41, AND

$$C'(x) = C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-1) \cdot x^{-2}\right)$$

$$= C \left(\frac{5}{2} \cdot 2x + 64 \cdot (-$$

$$C''(x) = c\left(5 - 64 \cdot (-2) \cdot x^{-3}\right) = c\left(5 + \frac{128}{x^2}\right) > 0$$

$$C(x) \qquad \text{Grave up}$$

$$\text{Since concave up}$$

$$\text{Incal nin is also the global nin}$$

$$x^{2}y = 16 ft^{3}$$
 = 7 use the constraint to find y

 $x = \frac{4}{3\sqrt{5}}$
 $(\frac{4}{5\sqrt{3}})^{2}y = 16 \Rightarrow \frac{16}{5^{2/3}}, y = 16$
 $y = 5^{2/3} ft$.

The dimensions of the crate that MINIMIZE the cost of the materials are
$$\frac{4}{3\sqrt{5}}$$
 by $5^{\frac{2}{3}}$ ft.