

Scheduling and Motion Planning for Wireless Sensors and Mobile Networks

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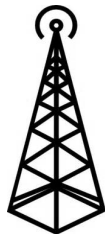
September 11th, 2017.

Research Interest and Projects

Computational Geometry, Algorithm Design and Analysis, Wireless Networks, Social Networks

- ▶ Geometric Methods for Network Analysis.
- ▶ Location and Trajectory Privacy.
- ▶ Social Influence and Contagions
- ▶ Scheduling Algorithms.

Scheduling Wireless Devices



Considerations:

- ▶ Efficiency – energy, storage, bandwidth.
- ▶ Performance – coverage, detection, connectivity.

Constraint dimensions:

- ▶ Spatial – visibility, proximity.
- ▶ Temporal – mobility.

Two Application Scenarios

How to schedule and allocate resources in spatial and temporal domains?

- ▶ Smart building: optimize energy usage, improve safety & security.

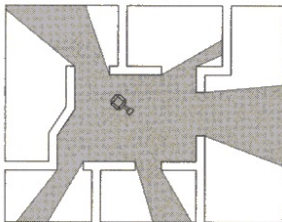
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- ▶ Smart building: optimize energy usage, improve safety & security.
- ▶ Mobile networks: assign mobile nodes to collect data from sensors with storage capacities.

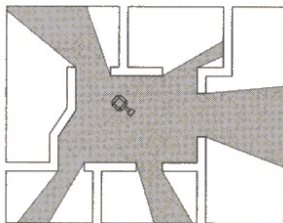
Coverage in Smart Building

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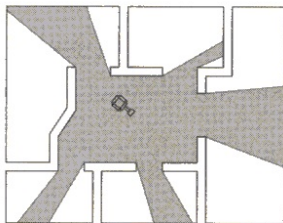
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- ▶ If sensors are turned on all the time: Art Gallery Problem;
- ▶ Sensors are not turned on all the time: Duty Cycle Scheduling.

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- ▶ Time is slotted.
- ▶ At each time slot at most k cameras are turned on.
- ▶ Minimize the maximum or average *dark duration*.
- ▶ Or, meet specific target coverage frequency requirements.

Scheduling for Minimizing Dark Duration

Given n camera nodes and m target nodes, the set of targets covered by sensors g_i is $P(g_i)$, suppose at any slot only k sensors are turned on, how to schedule sensors such that no target stays 'in dark' for too long.

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$S :$	g_1	g_2	g_3	g_2	g_1	g_2	g_3	g_2	...
	p_1				p_1				
	p_2	p_2		p_2	p_2	p_2		p_2	
		p_3		p_3		p_3		p_3	
			p_4				p_4		

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- ▶ **Min Average Dark Duration Scheduling:**

$$\min \sum_{p \in D} w(p) \cdot T(p)$$

where $w(p)$ is a weight parameter.

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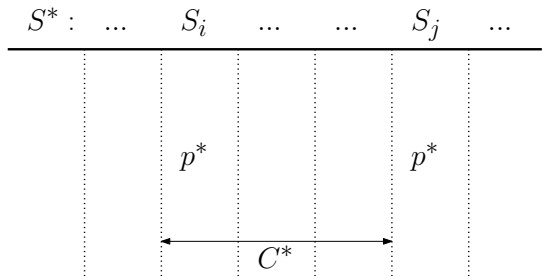
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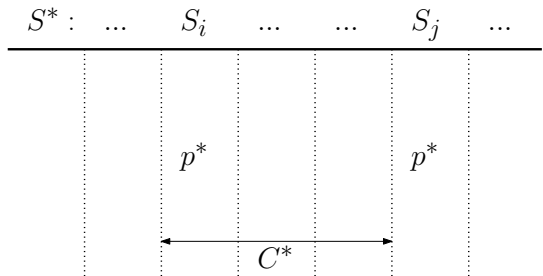


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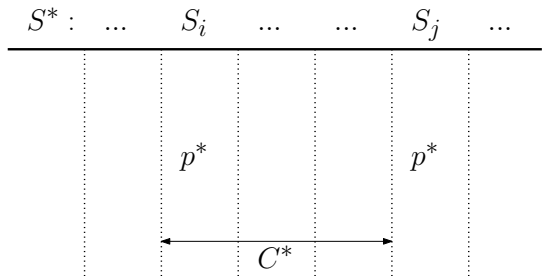
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Assume $C^* < \lceil n/k \rceil$ realized by $p^* \in D$.

Then at least one guard g does not appear during the interval of length C^* as shown below.

→ the point that is only guarded by g has dark duration $> C^*$.

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Min Max problem is tailored towards worst case & sensitive to outliers.

Min Average Dark Duration Scheduling: Motivation

Example:

- ▶ Three guards g_1, g_2, g_3 and six targets $p_1, p_2, p_3, p_4, p_5, p_6$.

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Min average optimization: use the weights $w(\cdot)$ to allow more flexibility to adjust to varying guarding requirements.

- ▶ Targets with higher importance have higher weights.

Algorithms for Min Average Dark Duration Scheduling

Challenge:

- ▶ Which sensor to repeat, and how many times?
- ▶ How to schedule them?

Special Case: Round Robin On a Permutation π

Find the optimal one π^* that minimizes the min average dark duration.

- ▶ Take a target $p \in D$, consider all guards that cover p we wish them to uniformly spread in π .

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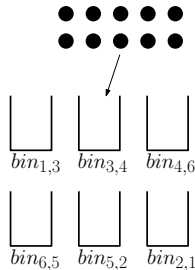
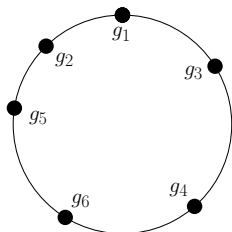
$$G(p) \subseteq V, |V| = 16$$

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$$G(p) = \{g_1, g_2, g_3, g_4, g_5, g_6\}$$

$$m = |G \setminus G(p)| \text{ balls}$$

Assume $G(p)$ appears in the permutation with this order $g_1, g_3, g_4, g_6, g_5, g_2$



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- ▶ Throw m balls randomly into ℓ bins, how many balls do we have in the largest bin?
- ▶ Compared to the optimal (uniform), the ratio is $\alpha = O(1)$ if $k \geq \log n / \log \log n$, and $\alpha = O(\log n / \log \log n)$ otherwise.

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The guards in one full cycle T of a periodic schedule: each guard g appears $\tau(g)$ times. Total # guards in one cycle is $\sum_g \tau(g) = Tk$.

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B is a convex function of $f(g)$ – we can minimize the right hand side!

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- ▶ Turn $f(g)$ into a nearby rational number and find $\tau(g), T$ such that $\tau(g)/(kT) \approx f(g)$.
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This algorithm gives $(2 + \varepsilon)\alpha$ approximation in expectation, $\alpha = O(1)$ if $k \geq \log n / \log \log n$, and $\alpha = O(\log n / \log \log n)$ otherwise.

Min Energy Scheduling with Target Coverage Frequency

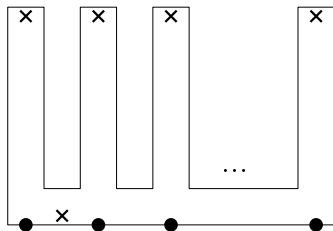
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Suppose target j needs to be covered every f_j slots, how to schedule sensors to meet the requirement such that at each slot only k sensors are turned on? Minimize k .

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Bottom target must be covered every slot while each of the top target must be covered every m slots.

Min Energy Scheduling with Target Coverage Frequency

Use set multi-cover & randomization. Details skipped.

- ▶ $O(\log n + \log m)$ approximation.
- ▶ Geometric setting: better approximation.

Part II: Path Planning for Mobile Nodes

Problem: Given a set of n sensor nodes $\{p_1, p_2, \dots, p_n\}$, schedule mobile nodes to serve them (data collection, battery recharging). Suppose the mobile node travels with unit speed.

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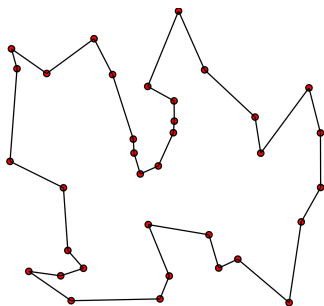
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Additional constraints: data rate/node capacity, time-window.

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- ▶ Theorem: The optimal solution is a zig-zag tour on an interval.
- ▶ Run Dynamic Programming in $O(n^2)$ time.

Data Collection Problem

With Sensors	Single mule	k -mule	No Data Loss
on a Line	in P	$\frac{1}{3}$	exact
on a Tree	pseudo-poly	$\frac{1}{3}(1 - 1/e^{\frac{1}{2+\varepsilon}})$	12
General Metric	$1/6 - \varepsilon$		
Euclidean	$1/3 - \varepsilon$		
Diff Capacities	$O(\frac{1}{m})$		$O(m)$

Table: $m \leq \log(\frac{c_{max}}{c_{min}})$ where c_{max} is the largest capacity and c_{min} is the smallest capacity. For the results in the first four rows, we assume that the sensor capacities are all the same. ε is any positive constant.

Example: Single Mule, Capacity c , Euclidean Setting

Algorithm:

- ▶ Find a path of length $c/2$ w/ max # R of nodes.
- ▶ Travelling back and forth along it gives a tour.
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- ▶ The interval has at most R *distinct* nodes.
- ▶ Total data collected from any sensor is c (on the first visit) and $c/2$ after each $c/2$ interval. Data rate is at most $3R$.

Conclusion

- ▶ Classical problems revisited.
- ▶ Worst-case performance guarantees.
- ▶ Optimization and scheduling are a crucial part of the machine intelligence era.

Acknowledgement

- ▶ Kin Sum Liu, Jie Gao, Shan Lin, Hua Huang, Brent Schiller, Joint Sensor Duty Cycle Scheduling with Coverage Guarantee, MobiHoc'2016.
- ▶ Kin Sum Liu, Tyler Mayer, Hao Tsung Yang, Esther Arkin, Jie Gao, Mayank Goswami, Matthew P. Johnson, Nirman Kumar, Shan Lin, Joint Sensing Duty Cycle Scheduling for Heterogeneous Coverage Guarantee, INFOCOM'2017.
- ▶ Gui Citovsky, Jie Gao, Joseph Mitchell, Jiemin Zeng, Exact and Approximation Algorithms for Data Mule Scheduling in a Sensor Network, ALGOSENSORS 2015.
- ▶ <http://www3.cs.stonybrook.edu/~jgao/>
- ▶ Questions and comments?